

$$\mathcal{Q}(\alpha, \beta, J, \mu) = \pi f(r, v) / m \quad (2)$$

is conserved along the bounce-averaged convection trajectory, where  $\alpha, \beta$  are the Euler potentials for labeling field lines,  $\mu, J$  are the first and second invariants, and  $f$  is the standard phase space density. An equivalent description in terms of the particle total energy is [eq. 41, *Northrop and Teller, 1960*],

$$n(\vec{r}, W, \mu) = 2BQ/v_{\parallel} \quad (3)$$

where  $W$  is the total energy defined above,  $v_{\parallel}$  is the parallel velocity, and  $n$  is the number of particles in  $d^3r$  at a given value of  $W, \mu$ .

### 3 ALGORITHMS AND RESULTS

To carry out this method for any  $K$  or equatorial pitch angle, we need an algorithm for calculating the functional dependence of  $B_m(K)$  on  $K$ . We do this numerically, (Figure 3), first mapping the field line from the equator to the ionosphere, here showing several longitudes collapsed into one display. We numerically integrate these  $B(s)$  curves to obtain the second adiabatic invariant  $K(s)$ . Note that on the day side, there are field lines which do not have a minimum at the equator, and thus  $K$  is undefined (imaginary) over some range of  $s$ . *Northrop and Teller [1960]* discuss this phenomenon, and like them, we find a generalized form of  $K$  defined as the sum of all non-imaginary  $K$ 's along a field line. With that definition, we calculate  $K$  from the minimum, either at the equator or elsewhere, to get  $K(s)$ . With these two quantities, we can now calculate  $B_m(K)$  as a polynomial expression, plotted in the final panel. We use 10th degree polynomials and arrive at an expression with less than 3% maximum deviation. Note that this is just an automated way of carrying out the Taylor and Hones graphical method, which we independently derived.

This part of the algorithm is the most time consuming, taking 5 hours on a SUN IPC for solving a 100 x 100 grid of the equatorial plane and using 200 integration steps along a field line. Once the polynomials are initialized, calculating a total energy for arbitrary  $K$  and  $\mu$ , which gives simultaneously every spatially distinct trajectory in the equatorial plane, required only 30 seconds, or only 3 seconds if  $\mu$  alone changes. This is to be contrasted with 3 minutes per single particle trace using a predictor-corrector method to time-integrate the forces.

Now that we have a realistic  $B(K)$  mapping, we also need to make  $U$  more realistic as well. *Pinto et al. [1987]* showed that drift trajectories would be greatly influenced by the ionospheric dynamo electric field [*Richmond et al., 1980*]. This dynamo field strengthens convection at low L-shells and compensates for the Volland-Stern shielding. However, the field is quadrupolar and topologically different from the dipolar Volland-Stern field, so that (Figure 2) in real space the tangent lines form a loop at low altitudes. When mapped into  $UB(K)$  space, the loop becomes a pleat, but only in the night half of the magnetosphere.

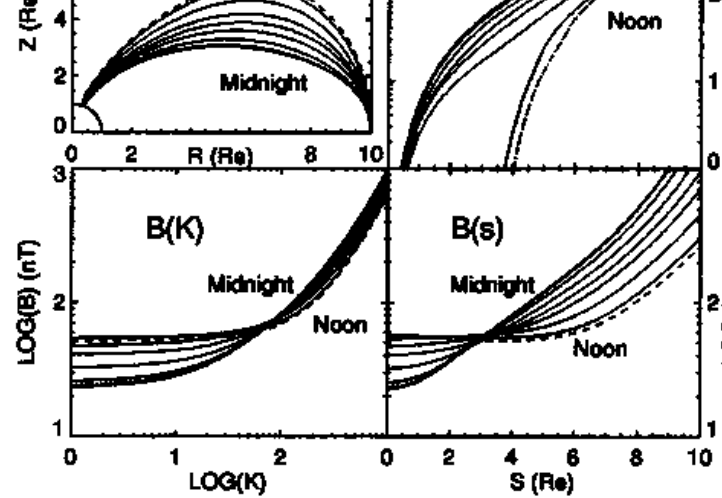


Fig. 3: a) Fieldlines traced from equatorial plane at 10 Re with longitude varying from midnight to noon in 20° increments; b)  $K(s)$  for fieldlines at 10 Re; c)  $B_m(K)$ , which is well defined for all fieldlines; and d)  $B(s)$  for fieldlines at 10 Re with an off equatorial minimum in the noon fieldline.

Since this is the first time trajectories have been shown for these realistic fields, we plot some examples in Figure 4. In panel (a), we see that for  $K=0$  or  $90^\circ$  equatorial pitch angles at a magnetic moment of 0.01 keV/nT, there are closed drift trajectories that do not encircle the earth [e.g., *Chen, 1970*], called “banana” orbits after tokamak usage [*Strangeway and Johnson, 1984*]. In  $UB(K)$  space these orbits are straight lines that nest in a concavity of the lower tangency curves. Note that the extra loop supports a new class of banana orbits; however these banana orbits are inside normal, earth encircling trapped orbits and thus have no access to the open drift trajectories from the tail. In panel (b), we see that for  $K=100$ , the banana orbits merge and appear outside the normal trapped orbit region. This allows them to be readily filled by diffusion or Coulomb drag effects. More importantly, there exists an open drift orbit threading between the normal closed orbits and the banana orbits. Because of the large value of  $L$  at low altitudes, convecting tail particles on this open drift trajectory become more pancake-like as the pitch angle rotates toward  $90^\circ$ , panel (c), and equatorial  $n(\vec{r}_{eq}, W, \mu)$  increases. Panel (d) plots the change in  $B_{eq}/\sqrt{\mu(B_m - B_{eq})}$ , which is directly proportional to the change in  $n(\vec{r}_{eq}, W, \mu)$ . Since this orbit is open to the tail, unlike its near neighbors, it alone experiences an order of magnitude increase in  $n(\vec{r}_{eq}, W, \mu)$  for some specific range of  $W, \mu$ . This mechanism can explain the peaks seen in this vicinity by ISEE-1 [*Williams and Frank, 1984, Sheldon, 1993*].

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