

$$= \frac{D^M L^{10}}{\Omega_M^2 \Omega_1^2} (\Omega_T / \Omega_M)^{2+k} \quad \Omega_T < \Omega_M$$

where we have normalized to the standard magnetic diffusion coefficient at  $\Omega_1 = \Omega_T$  ( $E=100$  keV,  $L=7.5$ ), and  $l$ ,  $D^M$ ,  $k$ , and  $\Omega_M$  remain to be determined. For  $\Omega_T > \Omega_M$  we obtain the standard form for the magnetic diffusion coefficient as given by Fälthammer [1965],

$$D_{LL}^M \propto L^{6+2l} \mu^{2-l} = L^{10} \quad l' = 2 \quad (13)$$

Fälthammer [1966] also derived a result for fluctuations shorter than the drift period of the ions, ( $\tau_M < \tau_T$ , or equivalently,  $\Omega_T < \Omega_M$ ) and found  $l'=0$ . This corresponds to our second case above with a resonant frequency below the peak in the power spectrum if we take  $k \ll 1$ . This choice of a small value for  $k$  which implies a very flat  $H_1(\Omega_T)$  spectrum, is consistent with short pulses, since the narrower the pulsewidth, the broader the frequency spectrum. Thus our generalized spectrum is consistent with the two special cases considered by Fälthammer.

**Modified electric diffusion.** Fälthammer [1965] derives a relatively general result for the diffusion caused by electric fluctuations (his equation 3.10),

$$\langle (\Delta r)^2 \rangle = \frac{1}{4B_d^2(r)} \sum_{n=1}^N G_n(r, n\Omega(\mu, r)) \quad (14)$$

where  $B_d$  is the equatorial dipole field, and  $G$  (analogous to the magnetic fluctuation power  $H_1$  of (10)) is the cross correlation of the azimuthal electric field fluctuations. Only azimuthal fluctuations are considered here because the magnetic field is taken to be dipolar, without a cross-tail electric field, so that only azimuthal electric fields contribute to radial diffusion. In a real magnetosphere this is not entirely true, particularly for ring current energy ions below 100 keV, which because of their somewhat noncircular drift orbits can couple to the fluctuation power in the radial electric field component as well. Unfortunately, these complications are rather difficult to include in the azimuthally symmetric model used here, so we will treat the empirically calculated electric field power to be solely azimuthal fluctuations, recognizing that there is a radial fluctuation component to the diffusion also whose contribution depends on energy and location.

However the simplification of the  $G$  function to just the autocorrelation of azimuthal fluctuations does not survive intact. The assumption of large timescales,  $\tau \gg 1/\Omega_T$  (his equation A.17) is what justifies keeping only the autocorrelation of the electric field fluctuations. Without being able to make this simplifying assumption, which breaks down when the drift frequency approaches zero, we approximate with a parameterized spectral form composed of the sum of two power laws as above. This form is based on experimental measurements of the electric field power spectra made at  $L=6.2$  [Holzworth and Mozer, 1979],  $L=2.3$  [Andrews, 1980], and  $L=1$  [Earle and Kelley, 1987], which all show

does not generally know the global mode or the phase of the electric field fluctuations, so we make the assumption that all the power is in the fundamental, and that all the phases are random. We are not so much interested in reconstructing the modes of the electric field fluctuation as finding a fluctuation power spectral form that will adequately explain the observed diffusion. Thus we assume that the electric fluctuation power can be written

$$P_E(r, \Omega) = \sum_i \langle \Delta E_i^2(r) \rangle H_1(\Omega_T) \quad (15)$$

where  $\langle \Delta E_i^2 \rangle$  incorporates the radial dependence of the electric field fluctuations for each component  $i$  to allow for the possibility of multiple sources. As before, we model the electric fluctuation power by assuming there is some peak frequency in the spectrum,  $\Omega_E$  with power law falloff both higher and lower frequencies. With these approximations we can write [e.g., Cornwall, 1968]

$$D_{LL}^E = \frac{\sum_i \langle \Delta E_i^2 \rangle}{8B_d^2} (\Omega_T / \Omega_E)^{-n} \quad \Omega_T \geq \Omega_E$$

$$= \frac{\sum_i \langle \Delta E_i^2 \rangle}{8B_d^2} (\Omega_T / \Omega_E)^m \quad \Omega_T < \Omega_E$$

where for simplicity we use the same spectral shape for all components.

### Modified Radial Gradients

The standard radial diffusion coefficient contains an external  $L^6$  radial dependence,  $D_{LL}^E \propto L^6 \langle \Delta E_{ext}^2 \rangle$ , because a nearly constant azimuthal  $\Delta E_{ext}$  fluctuation combined with a radially varying B field causes an  $\vec{E} \times \vec{B}$  radial deflection of  $\Delta E_\phi / B_d$ . A radially dependent fluctuation amplitude  $\langle \Delta E^2 \rangle$ , could in principle produce any desired radial dependence in the electric diffusion coefficient, which is not possible with magnetic fluctuations since currents produce global effects on the magnetosphere. That is, a sudden onset of compression of the magnetosphere does not locally compress the magnetosphere but globally, and the  $\Delta B$  fluctuation created (and its induced electric field) does not possess any strong  $L$  dependence. Because magnetic field lines are considered equipotentials (no parallel currents), the situation is different for electrostatic fluctuations. The potential difference between neighboring field lines is only limited by the ionospheric conductances, so that strong radial longitudinal gradients in the electrostatic potential are possible. We suggest three possible mechanisms for such spatial gradients: plasma shielding (space charge), divergence of magnetic field lines, and latitude-dependent sources.

In the Volland-Stern shielded electric field model [Volland, 1973; Stern, 1973] the ring current shields the external ( $L > 7.5$ ) voltage source (via charge separation between the counterrotating energetic ions and electrons [Vasyliunas, 1972]) so that this electric field weakens at lower altitudes. In this model, the external electric field is proportional to radial distance,  $E_{ext} \propto r$ , so that fluctuations in this high