

ANALYSIS

This region of the magnetosphere is characterized by stably trapped plasma, and thus adiabatic invariants of the motion are well conserved. In the absence of wave-particle scattering or collisions, an ion will conserve its total energy as it convects through this region. If the time rate of change of the magnetic field is small enough, $dB/dt = 0$, we can use a scalar field, U , to describe the electrostatic potential energy. With these assumptions, the total ion energy can be written, $W = K.E. + P.E. = \mu B_m + qU$, where μ is the magnetic moment, the first adiabatic invariant; B_m is the mirror point magnetic field strength, which depends on J , the second adiabatic invariant; and q is the charge. If the field lines are equipotentials, then B_m depends only on K , where $K = J/\sqrt{2m\mu}$. Thus given a B and E field model and specifying μ , K determines the equipotentials for all spatially distinct trajectories in the inner magnetosphere /9/. These equipotentials can be further simplified by making a coordinate transformation. Since $dW/dt = 0$, we can write, $\partial U/\partial B(K) = -\mu/q$. So that if we use $U, B(K)$ to label spatial coordinates, (mapping $r, \phi \rightarrow U, B$), then particle trajectories are straight lines whose slope depends only on the ratio of two constants /10/.

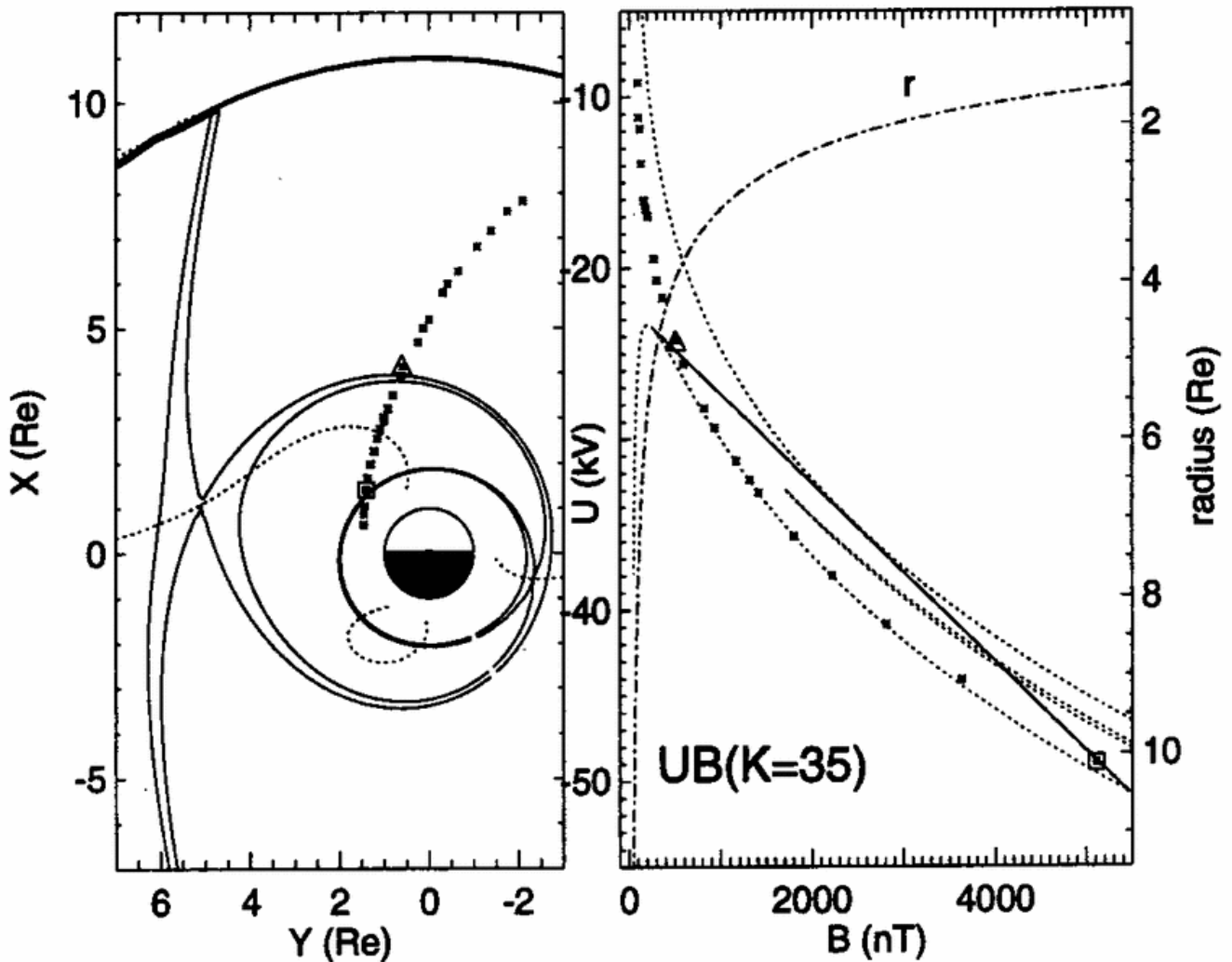


Fig. 1: 17 November 1977 ISEE-1 orbit shown in real space and $UB(K=35)$ space with asterisks; solid line is ion drift trajectory; U, B tangency points shown dotted.

The mapping for the first orbit is shown in Figure 1, where we calculate trajectories for an Olson-Pfizer /11/ magnetic field (standoff distance = $10.5 R_E$, $D_{st} = -31$) with a Volland-Stern + Richmond et al. /5/ electric field both in real space and transformed into $UB(K)$ space. We have used a value of $K = 35 R_E \cdot \sqrt{nT}$, corresponding to an equatorial pitch angle of 66° at $L=2$. The Volland-Stern